



# Course Specification (Postgraduate)

**Course Title:** Stability Theory of Differential Equations

Course Code: 202658-3

**Program:** Master of Pure Mathematics

**Department:** Mathematics

**College:** Science

Institution: Taif university

Version: 1

Last Revision Date: 21\10\2023







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## A. General information about the course:

#### **1. Course Identification:**

#### 1. Credit hours: (3)h

#### 2. Course type

Α.	□University	□College	□Department	□Track	
В.	□Required		⊠ Elec	tive	
<b>3.</b> L	evel/year at wh	ich this course is	s offered: (	Third level)	

#### 4. Course general Description:

Theory of general systems – properties of linear systems - stability of systems – Perturbation method – Lyapunov function - periodic solutions and approximations of periodic solutions.

5. Pre-requirements for this course (if any):

None

#### 6. Pre-requirements for this course (if any):

None

#### 7. Course Main Objective(s):

- 1. Understanding the concept of stability of systems and equilibrium points
- 2. Using different methods to determine the stability of the periodic solutions of linear and nonlinear differential equation.
- 3. Using perturbation method and Lyapunov function
- 4. Perception of some applications of ordinary differential equations in different field in science.

#### 2. Teaching Mode: (mark all that apply)

No	Mode of Instruction	Contact Hours	Percentage
1	Traditional classroom	3	100%
2	E-learning	0	0
	Hybrid		
3	Traditional classroom	0	0
	E-learning		
4	Distance learning	0	0





## 3. Contact Hours: (based on the academic semester)

No	Activity	Contact Hours
1.	Lectures	45
2.	Laboratory/Studio	0
3.	Field	0
4.	Tutorial	0
5.	Others (specify)	0
	Total	45

# B. Course Learning Outcomes (CLOs), Teaching Strategies and

## **Assessment Methods:**

Code_	Course Learning	Code of CLOs aligned	Teaching	Assessment
couc	Outcomes	with program	Strategies	Methods
1.0	Knowledge and unders	standing		
1.1	Recognizethedefinitionsandhavedeeperunderstandingoftheconceptofstabilityof systems andequilibrium points.	K1	-Lectures -Group Discussions	-Assignments -Exams
1.2	Identifydifferentmethod to determinethe stability ofequilibrium points oflinear and nonlineardifferential equations,	К2	-Lectures -Group Discussions	-Assignments -Exams
1.3	<b>Explain</b> concepts of perturbation method and Lyapunov function	К3	-Lectures -Group Discussions	-Assignments -Exams
2.0	Skills			
2.1	Applydifferentmethods to determinethestabilityofequilibriumpointslinearandnonlinearsystemsofordinarydifferential equation	<b>S1</b>	-Lectures -Group Discussions	-Assignments -Exams
2.2	<b>Employ</b> the suitable methods for estimating the stability of a	S2	-Lectures -Group Discussions	-Assignments -Exams





Code	Course Learning Outcomes	Code of CLOs aligned with program	Teaching Strategies	Assessment Methods
	system of ordinary differential equation.			
2.3	Explain the perturbation method and Lyapunov function and periodic solutions of the system of ordinary differential equation.	53	-Lectures -Group Discussions	-Assignments
3.0	Values, autonomy, and	d responsibility		
3.1	Accept critical thinking, communication skills, and the stability of the differential equations.	V1	-Projects	-Reports -Presentation
3.2	<u>Participate</u> the capability to use programing in solving differential equations systems problems.	V2	-Projects	-Reports -Presentation
	<u>Give</u> ability of self- learning and self- assessment during solving mathematical problems	V3	-Projects	-Reports -Presentation

# **C.** Course Content:

No	List of Topics	Contact Hours
1	Review of Higher Order Linear Equations and linear Systems: fundamental solutions, Wronskian, variation of constants, matrix exponential solution, behavior of solutions,	9
2	Linear Systems with Periodic Coefficients, Abel Liouville formula, Lagrange Identity, Green's Formula.	9
3	Phase Plane, Paths and Critical Points, Types of Critical points, Basic-Theorems on Stability, Application to Dynamics, Dependence on a Parameter,	9
4	Perturbation method and Lyapunov's Direct Method, stability theorems of system about critical points, Limit Cycles and Periodic Solutions,	9
5	Bendixson's Nonexistence Criterion, Poincare-Bendixson Theorem,	9





<b></b>	The Index of a Critical Point.	
	Total	45

# **D. Students Assessment Activities:**

No	Assessment Activities *	Assessment timing (in week no)	Percentage of Total Assessment Score
1.	Quizzes and HomeWorks	Continues	10 %
2.	Midterm exam	9 <sup>th</sup> -10 <sup>th</sup>	20 %
3.	Final exam	16 <sup>th</sup>	70%

\*Assessment Activities (i.e., Written test, oral test, oral presentation, group project, essay, etc.)

# E. Learning Resources and Facilities:

# **1. References and Learning Resources:**

Essential References	Nonlinear Dynamics and Chaos. By: Strogatz
Supportive References	<ol> <li>G. Birkhoff and G.C., Rota. Ordinary Differential Equations, John Wiley and Sons inc., NY, 1978.</li> <li>S. L. Ross. Differential Equations, John Wiley and Sons inc., NY, 1984.</li> <li>D. Somasundaram. Ordinary Differential Equations, Narosa Publishing House, Chennai, 2008.</li> <li>G. F. Simmons. Differential Equations with Applications and Historical Notes, McGraw Hill, 1991.</li> </ol>
	5. Differential equations, dynamical systems and an introduction to chaos By: Smale and Devaney
	6- Nonlinear oscillations 1973
	7-Problems in perturbations
Electronic Materials	
Other Learning Materials	

## 2. Educational and Research Facilities and Equipment Required:

Items	Resources
facilities	Classrooms containing whiteboard and electronic monitors
(Classrooms, laboratories, exhibition rooms,	
simulation rooms, etc.)	Computer laboratory equipped with hardware and software. Math software (MATLB, LaTeX)





Items	Resources
<b>Technology equipment</b> (Projector, smart board, software)	Laptop- Smart board- Projector.
<b>Other equipment</b> (Depending on the nature of the specialty)	Wi Fi internet connection.

## F. Assessment of Course Quality:

Assessment Areas/Issues	Assessor	Assessment Methods
Effectiveness of teaching	Students	Indirect
Effectiveness of students assessment	Students	Indirect
Quality of learning resources	Students	Indirect
The extent to which CLOs have been achieved	Peer reviewer	Direct
Other		

Assessor (Students, Faculty, Program Leaders, Peer Reviewer, Others (specify) Assessment Methods (Direct, Indirect)

# **G. Specification Approval Data:**

COUNCIL /COMMITTEE	
REFERENCE NO.	
DATE	21/10/2023

قسم الرياضيا<mark>ت والإحصاء</mark> Mathematics and Statistics Department



